

**CHEM 302**  
**Assignment #2**

Provide solutions to the following questions in a neat and well organized manner, including dimensional analysis, where appropriate.

Reference data sources for any constants and state assumptions, if any.

Due: Thursday, October 12<sup>th</sup>, 2017

1. Use the barometric pressure equation below to calculate the pressure and number density in the upper stratosphere at 35 km altitude. Why is the relative abundance of atomic oxygen greater in the upper stratosphere relative to the lower stratosphere? What impact does this have on the residence time of O<sub>3</sub> in the upper stratosphere?

$$P_h = P^o e^{-\left(\frac{\bar{M}_{air}gh}{RT}\right)}$$

where  $\bar{M}_{air} = 0.02896 \text{ kg mol}^{-1}$   
 $g = 9.81 \text{ m s}^{-2}$   
 $h = 35,000 \text{ m}$   
 $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$   
 $T = 240 \text{ K (Fig 2.1)}$

} in S.I. units

$$\therefore \frac{\bar{M}_{air} \cdot g \cdot h}{RT} = \frac{(0.02896)(9.81)(35,000)}{(8.314)(240)} = 4.98$$

$\left[ \begin{array}{c} \frac{\text{kg}}{\text{mol}} \cdot \frac{\text{m}}{\text{s}^2} \cdot \text{m} \\ \hline \frac{\text{J}}{\text{mol K}} \cdot \text{K} \end{array} \right]$

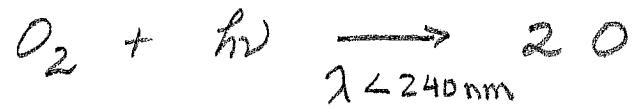
$$\therefore P_h = (1.00 \text{ atm}) e^{-4.98} = 6.85 \times 10^{-3} \text{ atm} \quad \text{or} \quad 694 \text{ Pa}$$

$$n_h^* = n_0^* e^{-4.98} = \left( \frac{PV}{RT} \cdot N_A \right) e^{-4.98}$$

$$= 3.057 \times 10^{19} \frac{\text{molecules}}{\text{cm}^3}$$

using  $T = 240 \text{ K}$

In the upper stratosphere, the relative abundance of atomic oxygen increases under the influence of increased solar flux of short wavelength (high energy) UVb and UVC light.

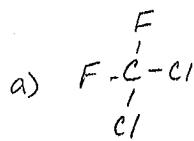


With higher concentrations of atomic O,  
the rate of O<sub>3</sub> production will increase.

Since O<sub>3</sub> is present at some steady state amount in stratosphere, its' rate of destruction will increase as well.

With higher rates of prod'n & destruction,  
the residence time of O<sub>3</sub> will decrease.

2. In 1974, Rowland and Molina suggested that the only environmental *sink* for CFC compounds was transport to the stratosphere\*. The refrigerant known as Freon 12 (dichlorodifluoromethane) has an atmospheric *residence time* of  $\sim 200$  yrs. Using the bond dissociation energies given in your text, calculate the maximum wavelength of light capable of photolyzing this compound. What additional information is required in order to predict rate of a photochemical reaction?



Bond enthalpies from Appendix B.3 (text)

$$\text{C-F} \quad 484 \text{ kJ/mol}$$

$$\text{C-Cl} \quad 338 \text{ kJ/mol} \quad \leftarrow \text{weakest bond}$$

$$E_{\text{photon}} = h\nu = \frac{hc}{\lambda} \quad \therefore \lambda \leq \frac{hc}{E_{\text{photon}}}$$

$$E_{\text{photon}} = 338 \times 10^3 \text{ J/mol} \times \frac{1 \text{ mol}}{6.02 \times 10^{23}} = 5.612 \times 10^{-19} \text{ J}$$

$$\therefore \lambda \leq \frac{(6.626 \times 10^{-34} \text{ Js})(3.00 \times 10^8 \text{ m s}^{-1})}{(5.612 \times 10^{-19} \text{ J})} = 3.542 \times 10^{-7} \text{ m}$$

$$\lambda \leq 354 \text{ nm}$$

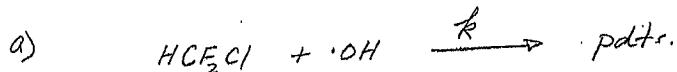
- b) Although photons of this wavelength are available in the troposphere, Freon-12 has no chromophore that absorbs light in this region. Therefore, this rxn' is limited to the stratosphere where even shorter  $\lambda$  light is available.

c) rate of photochemical reaction  
depends on conc: of absorbing species  
and the photochemical rate constant,  $f$ .  
 $\text{Rate} = f [A]$

$$f = \int_{\lambda_1}^{\lambda_2} \Phi_\lambda \sigma_\lambda J_\lambda d\lambda$$

The photochemical rate constant itself depends on the photochemical quantum yield ( $\Phi$ ), the absorption cross-section ( $\sigma$ ) and the photon flux ( $J$ ).

3. HCFC-22 is one of the compounds recommended as a replacement for CFCs. Its current tropospheric concentration is about 0.10 ppbv. It is known to react with tropospheric hydroxyl radical with a rate constant of  $4.0 \times 10^{-15} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$ .
- Using a constant value for the hydroxyl radical concentration of  $6.6 \times 10^5 \text{ molec cm}^{-3}$ , determine the rate of tropospheric oxidation via hydroxyl radical and estimate the tropospheric residence time of HCFC-22.
  - Draw the structure of HCFC-22 and suggest a reaction sequence consistent with its oxidation in the troposphere.



$$\text{Rate} = k [\text{HC}_2\text{Cl}] [\cdot\text{OH}]$$

$$\text{where } k = 4.0 \times 10^{-15} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$

$$[\cdot\text{OH}] = 6.6 \times 10^5 \text{ molec cm}^{-3}$$

$$[\text{HC}_2\text{Cl}] = \frac{0.10 \times 10^{-9} \text{ mol}}{1 \text{ mol air}} \times \frac{6.02 \times 10^{23} \text{ molec}}{1 \text{ mol}} \times \frac{1 \text{ mol/air}}{22.4 \text{ L}} \times \frac{1 \text{ L}}{10^3 \text{ cm}^3}$$

↑  
at STP

$$= 2.69 \times 10^9 \frac{\text{molec}}{\text{cm}^3}$$

$$\therefore \text{Rate} = (4.0 \times 10^{-15} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1})(6.6 \times 10^5 \text{ molec cm}^{-3})(2.69 \times 10^9 \frac{\text{molec}}{\text{cm}^3})$$

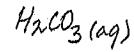
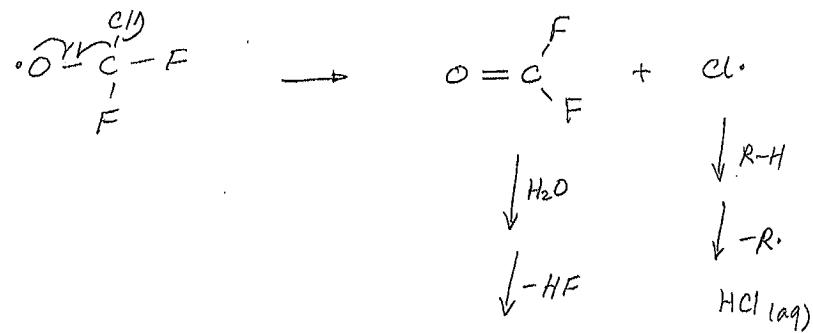
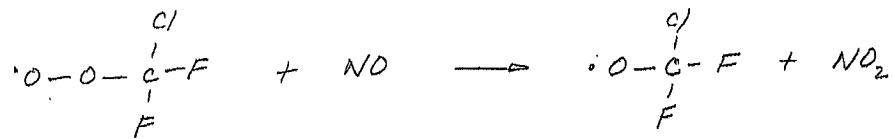
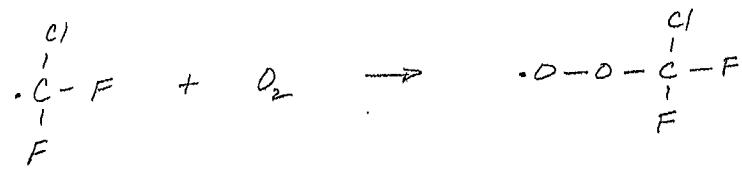
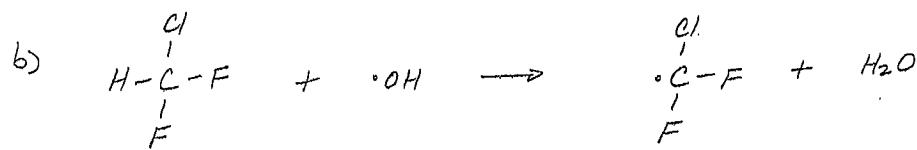
$$= 7.1 \frac{\text{molecules}}{\text{cm}^3 \cdot \text{s}}$$

$$\tau_{\text{trop}} = \frac{[\text{stock}]}{\text{Rate}} = \frac{1}{k[\cdot\text{OH}]} = \frac{1}{(4.0 \times 10^{-15} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1})(6.6 \times 10^5 \frac{\text{molec}}{\text{cm}^3})}$$

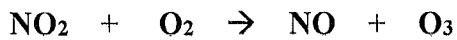
$$= 3.8 \times 10^8 \text{ s}$$

$\Rightarrow 12 \text{ yrs}$

(see further table 3.2  
text)



4. The following atmospheric reaction behaves as if it were first order with respect to  $\text{NO}_2$  with a *pseudo*-first order rate constant of  $2.2 \times 10^{-5} \text{ s}^{-1}$  at  $25^\circ\text{C}$ .



- a) Determine the second order rate constant ( $\text{molec}^{-1} \text{ cm}^3 \text{ s}^{-1}$ ) at  $25^\circ\text{C}$  and  $P_T = 1.00 \text{ atm}$ .  
 b) Assuming no new inputs of  $\text{NO}_2$  and no other loss processes, what percentage of  $\text{NO}_2$  remains after 60 mins?

a)  $\text{Rate} = k_{\text{obs}} [\text{NO}_2]$

where  $k_{\text{obs}} = k_2 [\text{O}_2] = 2.2 \times 10^{-5} \text{ s}^{-1}$  at  $298\text{K}$

$$\therefore k_2 = \frac{k_{\text{obs}}}{[\text{O}_2]}$$

$$\text{and } [\text{O}_2] = \frac{0.2095 \times 10^{-2} \text{ mol}}{1 \text{ mol/air}} \times \frac{6.02 \times 10^{23}}{\text{mol}} \times \frac{1 \text{ mol/air}}{24.5 \text{ L}} \\ \times \frac{1 \text{ L}}{10^3 \text{ cm}^3} \quad \begin{matrix} \uparrow \\ \text{at } 298\text{K} \\ P_T = 1.0 \text{ atm} \end{matrix} \\ = 5.15 \times 10^{18} \frac{\text{molec.}}{\text{cm}^3}$$

$$\text{So } k_2 = \frac{2.2 \times 10^{-5} \text{ s}^{-1}}{5.15 \times 10^{18} \frac{\text{molec.}}{\text{cm}^3}} = 4.3 \times 10^{-24} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$

b)

Conc  $\leftrightarrow$  time

$\therefore$  use integrated rate equation

$$\frac{[NO_2]_t}{[NO_2]_0} = e^{-k_{obs} \cdot t}$$

$$\text{where } k_{obs} = 2.2 \times 10^{-5} \text{ s}^{-1}$$

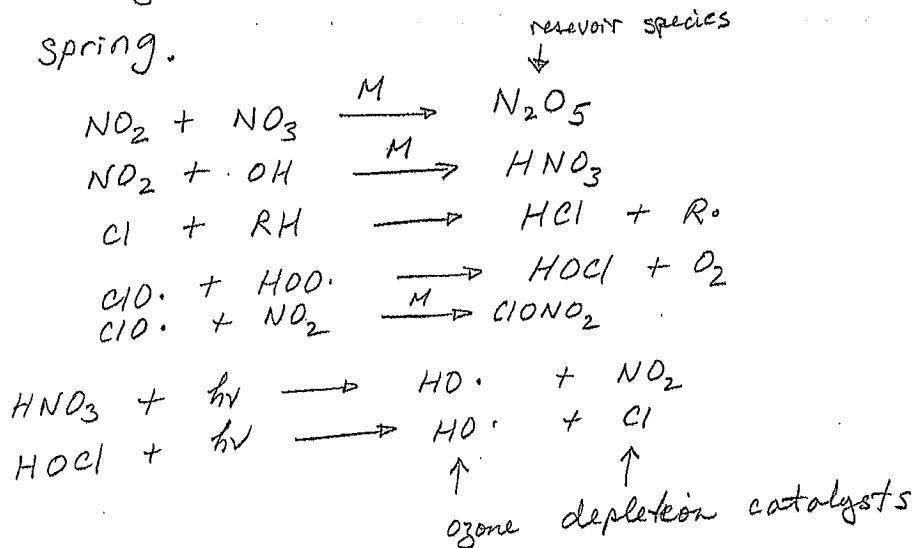
$$\begin{aligned} \text{and } t &= 60 \text{ mins} \\ &= 3.6 \times 10^4 \text{ s} \end{aligned}$$

$$\therefore \frac{[NO_2]_t}{[NO_2]_0} = e^{-0.0792} = 0.92$$

So after 60 mins, 92% of  $NO_2$  remains.

5. Explain what is meant by a 'holding cycles' and explain how these reactions can be related to polar stratospheric ozone depletion events. Illustrate your answer with examples from your textbook.

Holding cycles are reactions that convert reactive radical species into less reactive species that can be released later to take part in ozone depletion. The less reactive species are often referred to as reservoir species which can be transported greater distances due to their longer residence time. Polar stratospheric ozone depletion events are often driven by the photolysis of reservoir species which release ozone depletion catalysts (e.g. Cl<sup>•</sup>, NO<sub>2</sub> etc) during the polar spring.

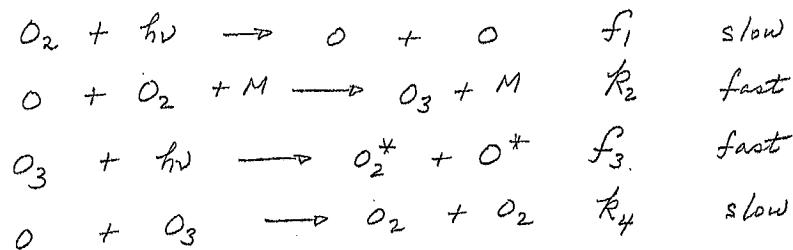


6. Applying the *steady state approximation* to O and O<sub>3</sub> in the Chapman reactions, it can be shown that;  $k_2[\text{O}_2][\text{O}][\text{M}] \approx f_3[\text{O}_3]$  and  $f_1[\text{O}_2] \approx k_4[\text{O}][\text{O}_3]$

Given the information below about the temperature dependence of the rate constants, predict the ozone concentration at 60 km altitude. The rate constants  $k_2$  and  $k_4$  vary with temperature as follows;

$$k_2 = 6.0 \times 10^{-34} \left( \frac{T}{300} \right)^{-2.3} \text{ cm}^6 \text{ molec}^{-2} \text{ s}^{-1} \quad k_4 = 8.0 \times 10^{-12} e^{\left\{ \frac{-2060}{T} \right\}} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$$

The photochemical rate constants  $f_1$  and  $f_3$  do not vary appreciably with temperature and are given by  $1 \times 10^{-11} \text{ s}^{-1}$  and  $1 \times 10^{-3} \text{ s}^{-1}$ , respectively.



$$k_2 [\text{O}_2] [\text{O}] [\text{M}] = f_3 [\text{O}_3]$$

$$\therefore [\text{O}_3] = \frac{k_2 [\text{O}_2] [\text{O}] [\text{M}]}{f_3}$$

$$\text{and } f_1 [\text{O}_2] = k_4 [\text{O}] [\text{O}_3]$$

$$\therefore [\text{O}] = \frac{f_1 [\text{O}_2]}{k_4 [\text{O}_3]}$$

$$\text{Therefore, } [\text{O}_3] = \frac{k_2 [\text{O}_2] \cdot \frac{f_1 [\text{O}_2]}{k_4 [\text{O}_3]} \cdot [\text{M}]}{f_3} = \frac{k_2 f_1 [\text{O}_2]^2 [\text{M}]}{k_4 f_3 [\text{O}_3]}$$

$$\therefore [\text{O}_3]^2 = \frac{k_2 f_1 [\text{O}_2]^2 [\text{M}]}{k_4 f_3} \Rightarrow [\text{O}_3] = \left( \frac{k_2 f_1}{k_4 f_3} \right)^{1/2} [\text{O}_2] [\text{M}]^{1/2}$$

Therefore,

$$[O_3] = \left[ \frac{(8.34 \times 10^{-34})(1 \times 10^{-11})}{(2.90 \times 10^{-15})(1 \times 10^{-3})} \right]^{1/2} (4.67 \times 10^{15}) (2.23 \times 10^{16})^{1/2}$$
$$= 3.7 \times 10^{10}$$

dimensional analysis:

$$\left[ \frac{\text{cm}^6 \text{ molec}^{-2} \text{ s}^{-1} \cdot \text{s}^{-1}}{\text{cm}^3 \text{ molec}^{-1} \text{ s}^{-1} \cdot \text{s}^{-1}} \right]^{1/2} \cdot \left[ \frac{\text{molec}}{\text{cm}^3} \right] \cdot \left[ \frac{\text{molec}}{\text{cm}^3} \right]^{1/2}$$
$$\Rightarrow \left[ \text{cm}^3 \text{ molec}^{-1} \right]^{1/2} \cdot \left[ \frac{\text{molec}}{\text{cm}^3} \right] \cdot \left[ \frac{\text{molec}}{\text{cm}^3} \right]^{1/2}$$
$$\Rightarrow \left[ \frac{\text{molec}}{\text{cm}^3} \right]$$

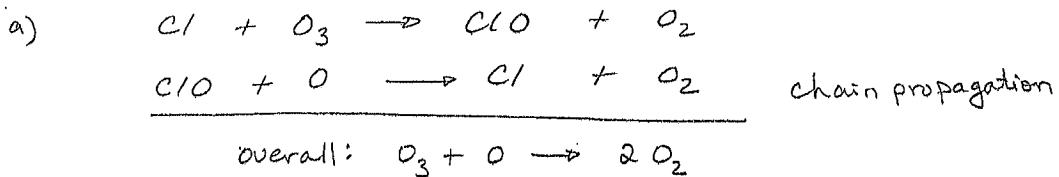
$$[O_3] = 3.7 \times 10^{10} \frac{\text{molec}}{\text{cm}^3}$$

7. An important reaction in the destruction of ozone is



The rate constant for this reaction as a function of temperature is given as  $k(T) = 2.9 \times 10^{-11} e^{-260/T}$ , in units of molecules<sup>-1</sup> cm<sup>3</sup> s<sup>-1</sup>.

- a) What is the rate of ozone destruction by this reaction at an altitude of 30 km near the Earth's equator, where the average atomic chlorine concentration is about  $4 \times 10^3$  molecules cm<sup>-3</sup>?
- b) How does this compare to the atmosphere above the Antarctic, where the temperature is about -80°C, the ozone concentration is  $2 \times 10^{11}$  molecules cm<sup>-3</sup> and the atomic chlorine concentration is about  $4 \times 10^5$  molecules cm<sup>-3</sup>.



b) rate  $O_3$  loss =  $k [Cl][O_3]$  at 30 Km,  $T \approx 240$  K  
 where  $k = 2.9 \times 10^{-11} e^{-260/240}$   
 $= 9.8 \times 10^{-12} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$

$$\begin{aligned} [O_3] &= 10^{12.2} \\ &= 1.6 \times 10^{12} \frac{\text{molec}}{\text{cm}^3} \end{aligned}$$

and  $[Cl] = 4 \times 10^3 \text{ molec/cm}^3$  Fig. 2.1

and  $[O_3] = 1.6 \times 10^{12} \text{ molec/cm}^3$

$\therefore$  Rate =  $6.2 \times 10^4 \text{ molec cm}^{-3} \text{ s}^{-1}$

c)  $k = 2.9 \times 10^{-11} e^{-260/193} = 7.4 \times 10^{-12} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1}$

$\therefore$  Rate =  $5.9 \times 10^5 \text{ molec cm}^{-3} \text{ s}^{-1}$

About 10 times faster  $O_3$  destruction above Antarctic.

8. An individual who hasn't taken CHEM 302 is running their old lawnmower in their garage (don't ask). The lawnmower is spewing carbon monoxide at a rate of 11 g/hr and the garage (which has a volume of 90 m<sup>3</sup>) is being ventilated such that the residence time of the air in the garage is 3.3 hr. Let us assume that the CO is lost from the garage by two processes: first, by simple flushing as it mixes with the clean ventilated air and second by some unspecified decay process with a rate constant of 5.6 × 10<sup>-5</sup> s<sup>-1</sup>. Under these conditions estimate the *residence time* (in hrs) and *steady state concentration* (ppm<sub>v</sub>) of CO in the garage.

$T_{vent} = 3.3 \text{ hr}$   
 $11 \text{ g/hr}$

$\rightarrow$

$V_{vol} = 90 \text{ m}^3$

$\rightarrow$

$k_{vent} = 0.30 \text{ hr}^{-1}$

$\rightarrow$

$k_{decay} = 5.6 \times 10^{-5} \text{ s}^{-1} \times \frac{3600 \text{ s}}{\text{hr}} = 0.20 \text{ hr}^{-1}$

$$T_{overall}^{CO} = \frac{1}{\sum k} = \frac{1}{k_{vent} + k_{decay}} = \frac{1}{(0.30 + 0.20) \text{ hr}^{-1}}$$

$$= 2.0 \text{ hr}$$

$$T_{overall}^{CO} = \frac{\text{stock}}{\text{flux}} \quad \text{and @ steady state, flux} = 11 \text{ g/hr}$$

$$\therefore \text{stock} = (T_{overall}^{CO})(\text{flux}) = (2.0 \text{ hr})(11 \text{ g/hr}) = 22 \text{ g}$$

$$\therefore [CO]_{ss} = \frac{22 \text{ g}}{90 \text{ m}^3} \times \frac{1 \text{ mol}}{28 \text{ g}} \times \frac{22.41 \text{ L}}{1 \text{ mol/air}} \times \frac{1 \text{ m}^3}{10^3 \text{ L}} \times 10^6$$

$$= 112.5 \text{ ppm}_v$$

$$\Rightarrow 110 \text{ ppm}_v \text{ CO}$$