

Indoor Air and Air Exchange Rates

The air exchange rate (sometimes referred to as the number of air changes per hour "ach") is a first order rate constant (k_e) for the ventilation of indoor air. It is related to the indoor air residence time (τ_e) as $k_e = 1/\tau_e$.

Taking into account air exchange processes only (i.e., no chemical loss mechanisms);

$$\text{Rate of infiltration of an outdoor contaminant} = \frac{d[X]}{dt} = k_e [X]_{\text{outside}}$$

$$\text{Rate of ventilation of an indoor contaminant} = \frac{d[X]}{dt} = -k_e [X]_{\text{inside}}$$

Taking into account both infiltration from outdoor sources and ventilation of indoor sources, the net rate of accumulation of a contaminant inside is given by;

$$\text{Rate} = d[X]/dt = k_e [X]_{\text{outside}} - k_e [X]_{\text{inside}}$$

The integrated form of the rate equation is given by;

$$\ln ([X]_o - [X]_i) = -k_e t + \text{Constant}$$

At steady state, Rate in = Rate out

$$\text{Rate in} = k_e [X]_{\text{outside}} + \text{Rate of emission from an internal source}$$

and, assuming no chemical loss;

$$\text{Rate out} = k_e [X]_{\text{inside}}$$

Hence, at steady state;

$$k_e [X]_{\text{inside}} = k_e [X]_{\text{outside}} + \text{Rate of emission from an internal source}$$

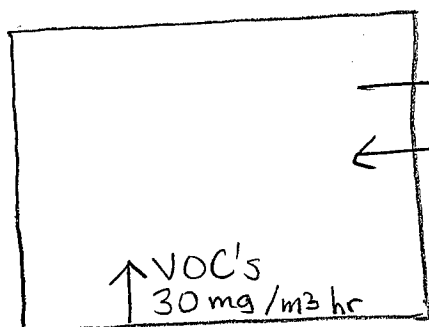
1. An open fire in a well ventilated home produces VOCs at a rate of $30 \text{ mg m}^{-3} \text{ h}^{-1}$. A complete exchange of air takes place every 5 minutes. The ambient outdoor air concentration of VOCs is $75 \text{ } \mu\text{g m}^{-3}$. Calculate the steady state indoor concentration of VOCs from this source assuming no chemical loss mechanisms.

[Answer = 2.6 mg m^{-3}]

complete exchange of air every 5 mins

$$\therefore \frac{60}{5} = 12 \text{ air changes per hour}$$

$$\text{so } k_e = 12 \text{ hr}^{-1}$$



$$k_e = 12 \text{ hr}^{-1}$$

$$[\text{VOC's}]_{\text{outside}} = 0.075 \frac{\text{mg}}{\text{m}^3}$$

$$\text{Rate VOC's out} = 12 \text{ hr}^{-1} [\text{VOC}]_{\text{in}}$$

$$\text{Rate VOC's in} = 12 \text{ hr}^{-1} [\text{VOC}]_{\text{out}} + 30 \frac{\text{mg}}{\text{m}^3 \text{ hr}}$$

$$= 0.90 \frac{\text{mg}}{\text{m}^3 \text{ hr}} + 30 \frac{\text{mg}}{\text{m}^3 \text{ hr}} = 30.9 \frac{\text{mg}}{\text{m}^3 \text{ hr}}$$

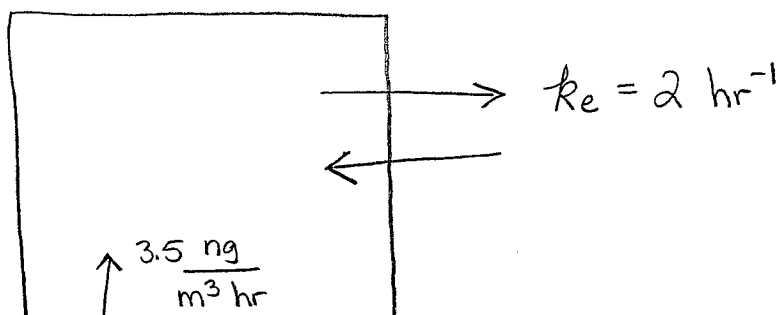
at steady state Rate in = Rate out

$$\therefore 12 \text{ hr}^{-1} [\text{VOC}]_{\text{in}} = 30.9 \frac{\text{mg}}{\text{m}^3 \text{ hr}}$$

$$\text{and } [\text{VOC}]_{\text{in}} = \frac{30.9 \frac{\text{mg}}{\text{m}^3 \text{ hr}}}{12 \text{ hr}^{-1}} = 2.57 \frac{\text{mg}}{\text{m}^3}$$

2. In some rural communities, heating and cooking are often done with open fires. If the rate of emission of PAHs from indoor combustion is $3.5 \text{ ng m}^{-3} \text{ h}^{-1}$ and the outdoor concentration of PAHs is 0.60 ng m^{-3} , estimate the steady state indoor air concentration of PAH compounds if the air exchange rate is 2 h^{-1} . Assume that the only loss mechanism is by air exchange.

[Answer = 2.4 ng m^{-3}]



$$\text{Rate in} = \frac{3.5 \text{ ng}}{\text{m}^3 \text{ h}} + 2 \text{ h}^{-1} \left(0.60 \frac{\text{ng}}{\text{m}^3} \right) = 4.7 \frac{\text{ng}}{\text{m}^3 \text{ h}}$$

$$\text{Rate out} = k_e [\text{PAH}]_{\text{in}} = 2 \text{ h}^{-1} [\text{PAH}]_{\text{in}}$$

At steady state :

$$4.7 \frac{\text{ng}}{\text{m}^3 \text{ h}} = 2 \text{ h}^{-1} [\text{PAH}]_{\text{in}}$$

$$\therefore [\text{PAH}]_{\text{in}} = 2.35 \frac{\text{ng}}{\text{m}^3}$$

3. A one compartment home of volume 330 m^3 has an infiltration rate of 0.25 ach with doors and windows closed. During an episode of photochemical smog, the outdoor concentration of PAN is 85 ppb_v . If the family remains indoors and the initial concentration of PAN inside is 18 ppb_v , how long will it take before the PAN concentration inside rises to 45 ppb_v .

[Answer = 2.0 hr]

To relate conc. to time, we must use the integrated form of the rate expression

$$\ln ([X]_0 - [X]_i) = -k_e t + \text{Const.}$$

we use the $t=0$ data to calculate the magnitude of constant

$$\text{at } t=0, [X]_0 = 85 \text{ ppb}_v, [X]_i = 18 \text{ ppb}_v$$

$$\therefore \text{Constant} = \ln(85-18) = 4.20$$

$$\text{at } t=?, [X]_0 = 85 \text{ ppb}_v, [X]_i = 45 \text{ ppb}_v$$

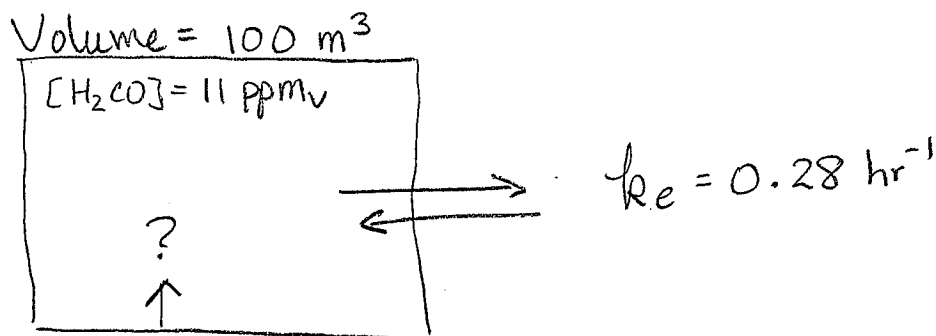
$$\therefore \ln(85-45) = -0.25 \text{ hr}^{-1} t + 4.20$$

$$\text{So } t = \frac{\ln(85-45) - 4.20}{-0.25 \text{ h}^{-1}}$$

$$= 2.0 \text{ hr}$$

4. A mobile home has a volume of 100 m^3 and a ventilation rate of 0.28 ach . If the concentration of formaldehyde in the home has reached a steady state concentration of 11 ppm_v , what is the rate of emission of formaldehyde from the materials in the home in mg per hour ?

[Answer = 38 mg h^{-1}]



Rate formaldehyde into home = Rate emission + Rate infiltration
 since outdoor conc of H_2CO not given, assumed to be very low (≈ 0)

$$\begin{aligned} \text{Rate out} &= k_e [\text{H}_2\text{CO}] = 0.28 \text{ h}^{-1} (11 \text{ ppm}_v) \\ &= 3.1 \text{ ppm}_v \text{ h}^{-1} \end{aligned}$$

\therefore At steady state, Rate emission = $3.1 \text{ ppm}_v \text{ h}^{-1}$

We need to convert this to mg per hour

$$\begin{aligned} &\frac{3.1 \times 10^{-6} \text{ mol H}_2\text{CO}}{1 \text{ mol air}} \times \frac{30,000 \text{ mg H}_2\text{CO}}{1 \text{ mol H}_2\text{CO}} \times \frac{1 \text{ mol air}}{24.45 \text{ L}} \times \frac{10^3 \text{ L}}{1 \text{ m}^3} \\ &= 3.8 \frac{\text{mg}}{\text{m}^3} \text{ per hour} \end{aligned}$$

$$\begin{aligned} \therefore \text{Rate H}_2\text{CO into home (emission source)} &= 3.8 \frac{\text{mg}}{\text{m}^3} \times 100 \text{ m}^3 \times \frac{1}{\text{hr}} \\ &= 38 \frac{\text{mg}}{\text{hr}} \end{aligned}$$